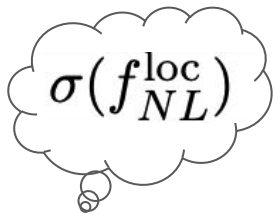
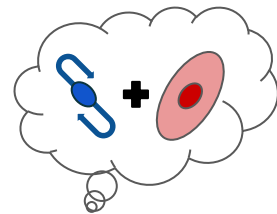


# Learning to Concentrate: Multi-tracer Forecasts on Local Primordial Non-Gaussianity with Machine-Learned Bias



*SPHEREx Cosmology Group*



Jamie Sullivan

(work w/ Tijan Prijon & Uroš Seljak)

arXiv:2303.08901

# Counting Inflationary Fields

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Initial gravitational potential largely Gaussian

But primordial physics can add non-Gaussianity (PNG)

E.g. multi-field inflation produces *local* PNG:

$$\phi = \phi_G + f_{NL}^{\text{loc}} [\phi_G^2 - \langle \phi_G^2 \rangle]$$

Measure this through local  $f_{NL}$

# Inflation in LSS via LPNG Bias

---

Planck has constrained local  $f_{NL}$  to be  $0.0 \pm 5.1$

But large-scale structure (LSS) has more modes

To get to galaxies, need a bias model:

$$\delta_g = b \delta + \dots \qquad \delta \propto k^2 \phi$$

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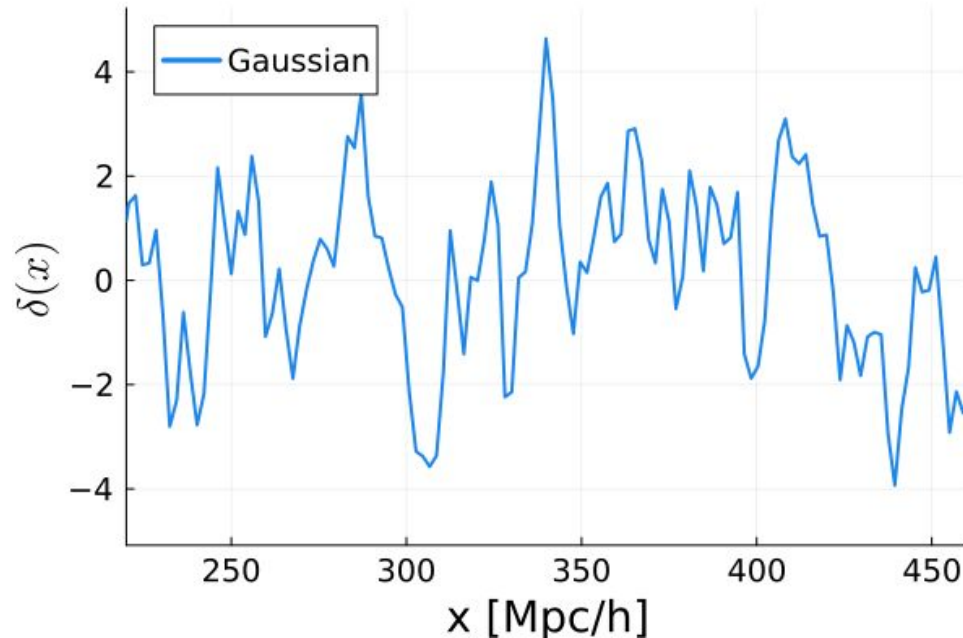
15 years ago, it was realized there is an **extra** bias signal

$$\delta_g = b \delta + \boxed{b_\phi f_{NL}^{(\text{loc})} \phi} + \dots$$

# Why extra bias? - Cartoon LPNG

LPNG “adds” long-wavelength potential mode

Long-wavelength potential “acts like local  $\sigma_8$ ”



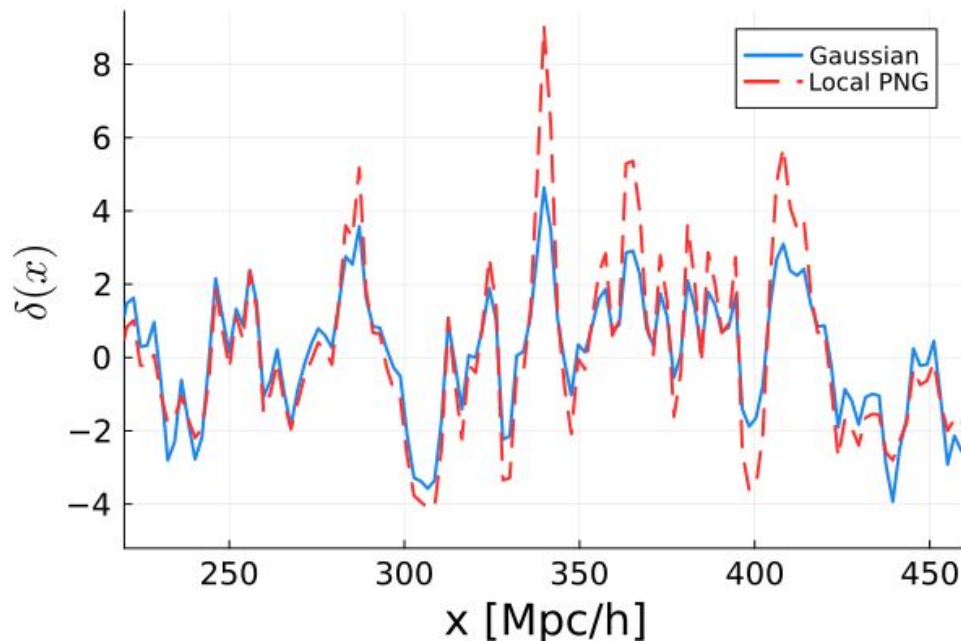
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Boosts variance

Affects halo formation



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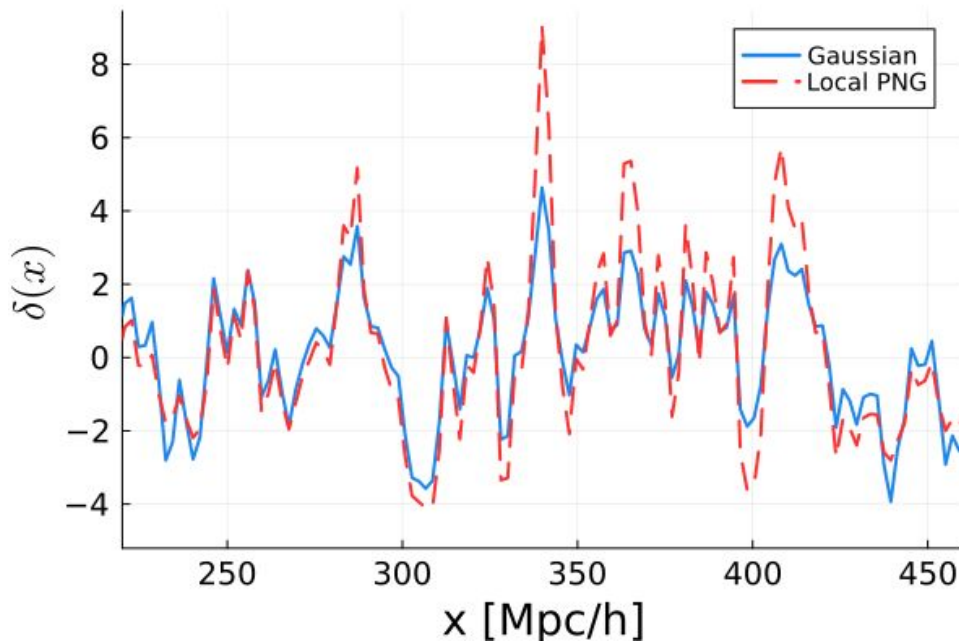
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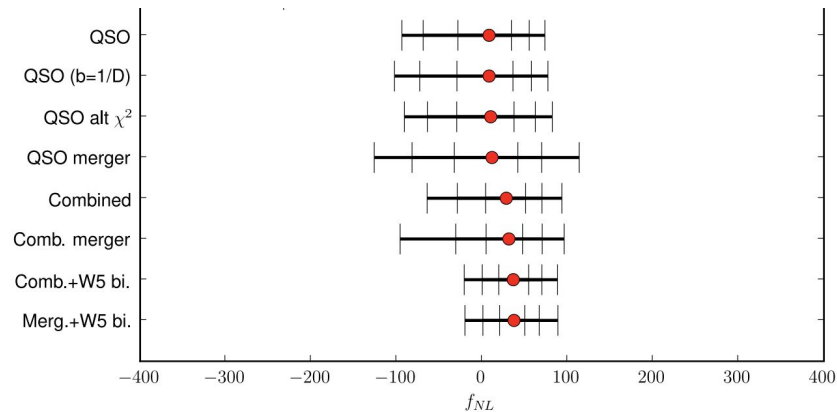
**And in data...?**





# LSS $f_{NL}^{(loc)}$ Constraints - SDSS quasars

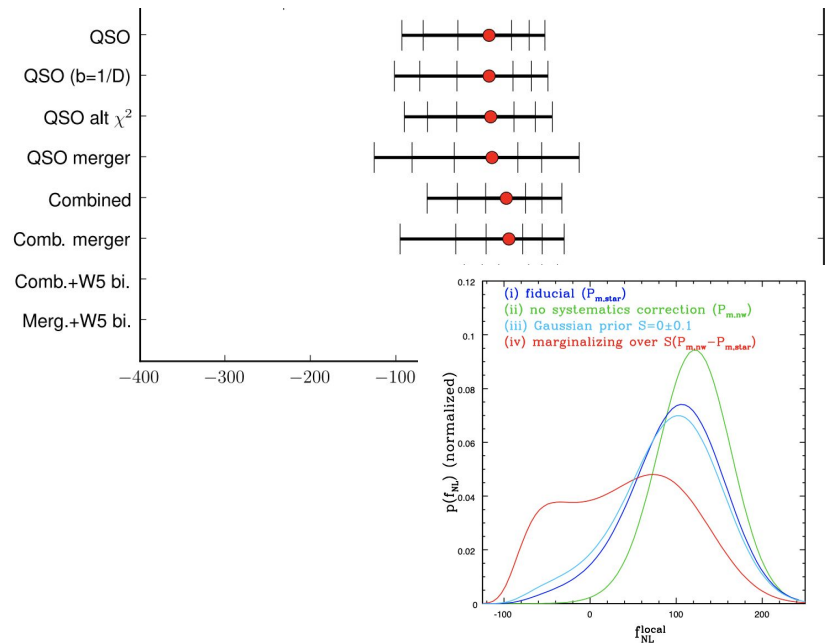
Slosar++08



# LSS $f_{NL}^{(loc)}$ Constraints - SDSS quasars

Slosar++08

Ross++12

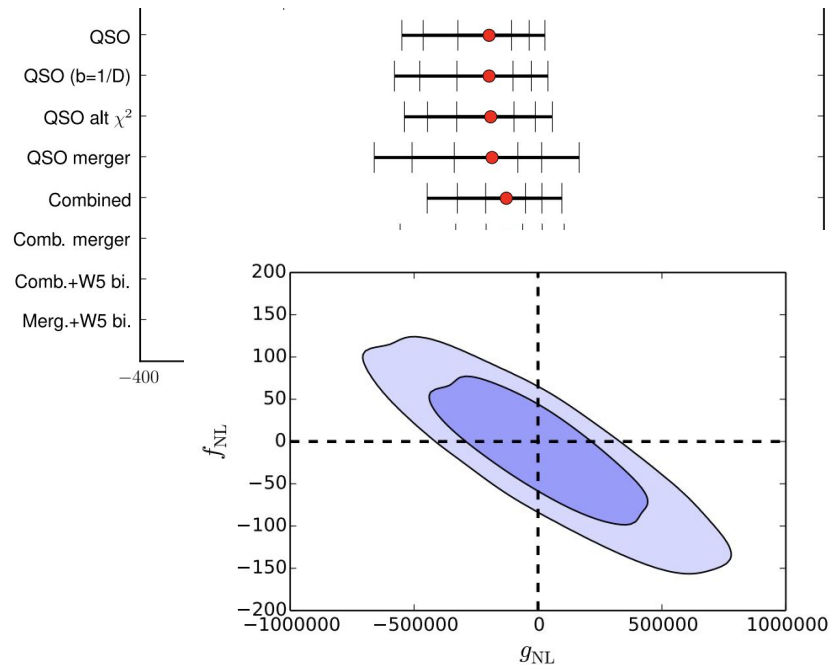


# LSS $f_{NL}^{(loc)}$ Constraints - SDSS quasars

Slosar++08

Ross++12

Leistedt++14



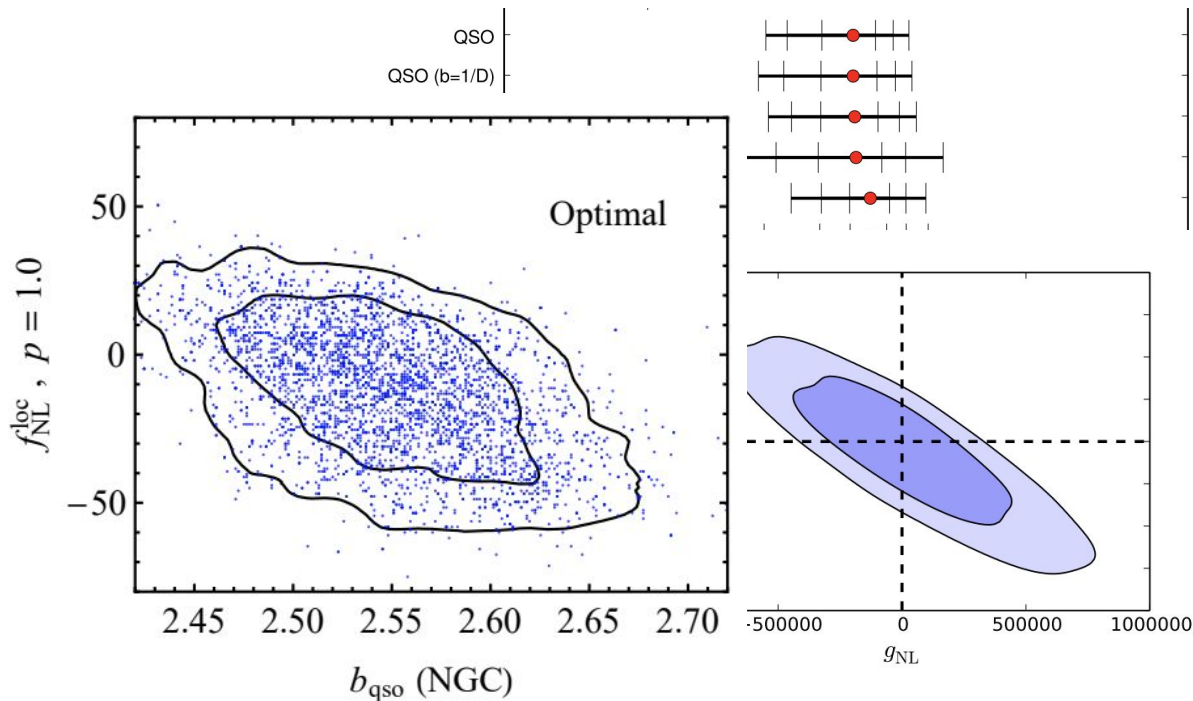
# LSS $f_{\text{NL}}^{\text{(loc)}}$ Constraints - eBOSS quasars

Slosar++08

Ross++12

Leistedt++14

Castorina++19



# LSS $f_{\text{NL}}^{\text{(loc)}}$ Constraints - eBOSS quasars

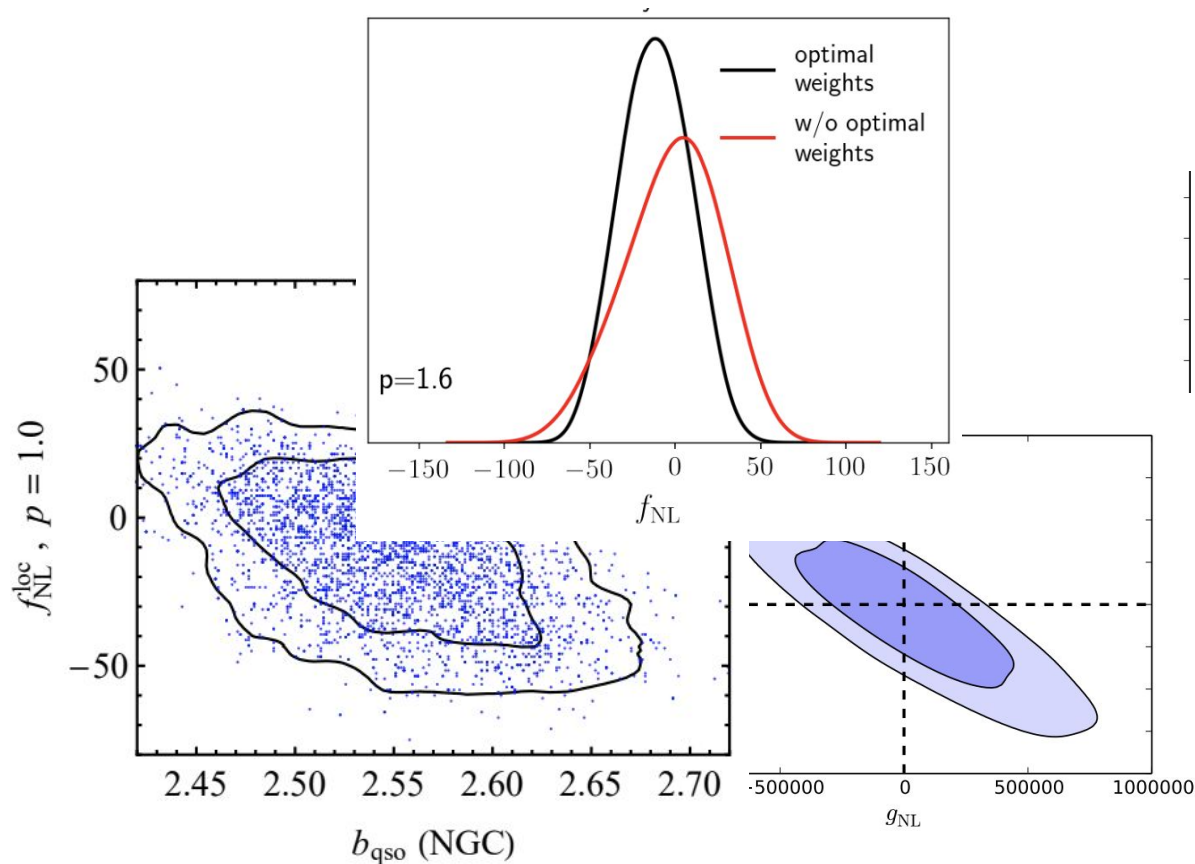
Slosar++08

Ross++12

Leistedt++14

Castorina++19

Mueller++21



# LSS $f_{NL}^{(loc)}$ Constraints - BOSS LRGs

Slosar++08

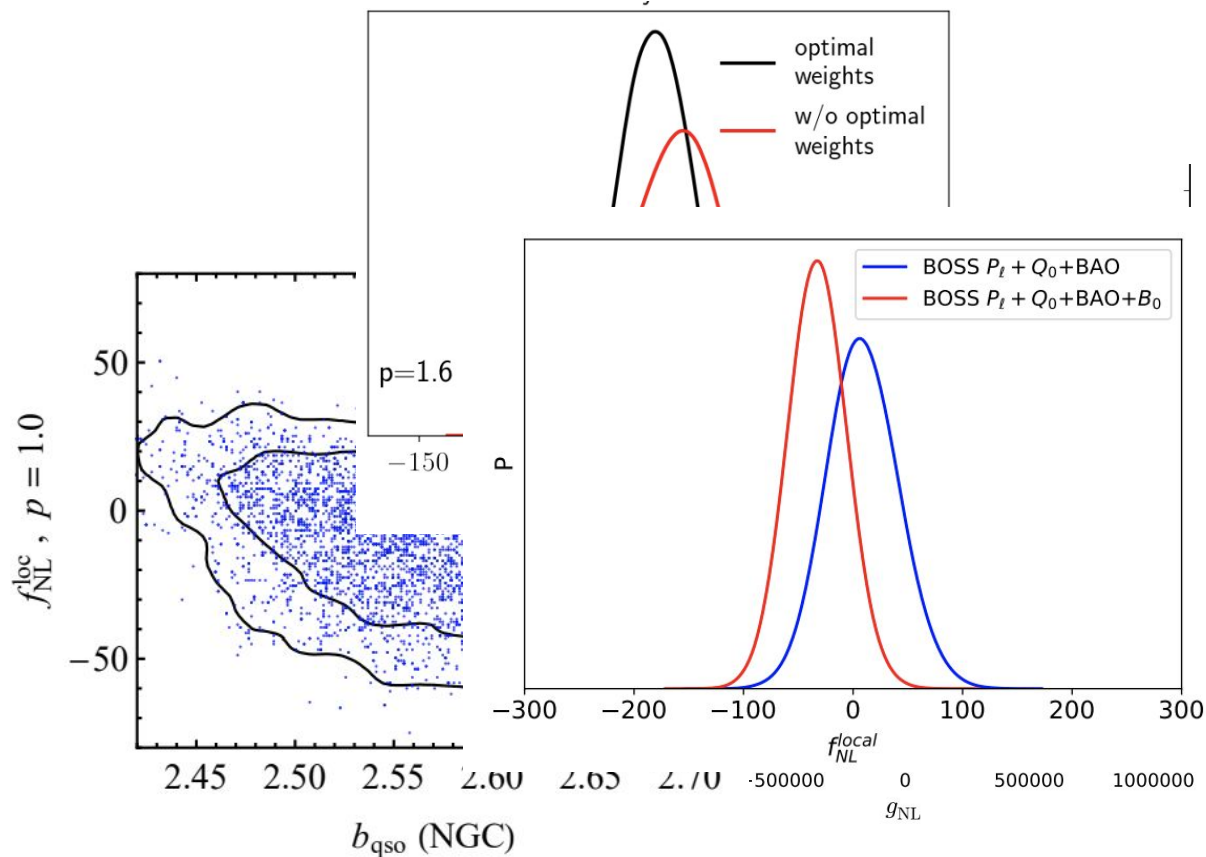
Ross++12

Leistedt++14

Castorina++19

Mueller++21

D'Amico++22



# LSS $f_{NL}^{(loc)}$ Constraints - BOSS LRGs

Slosar++08

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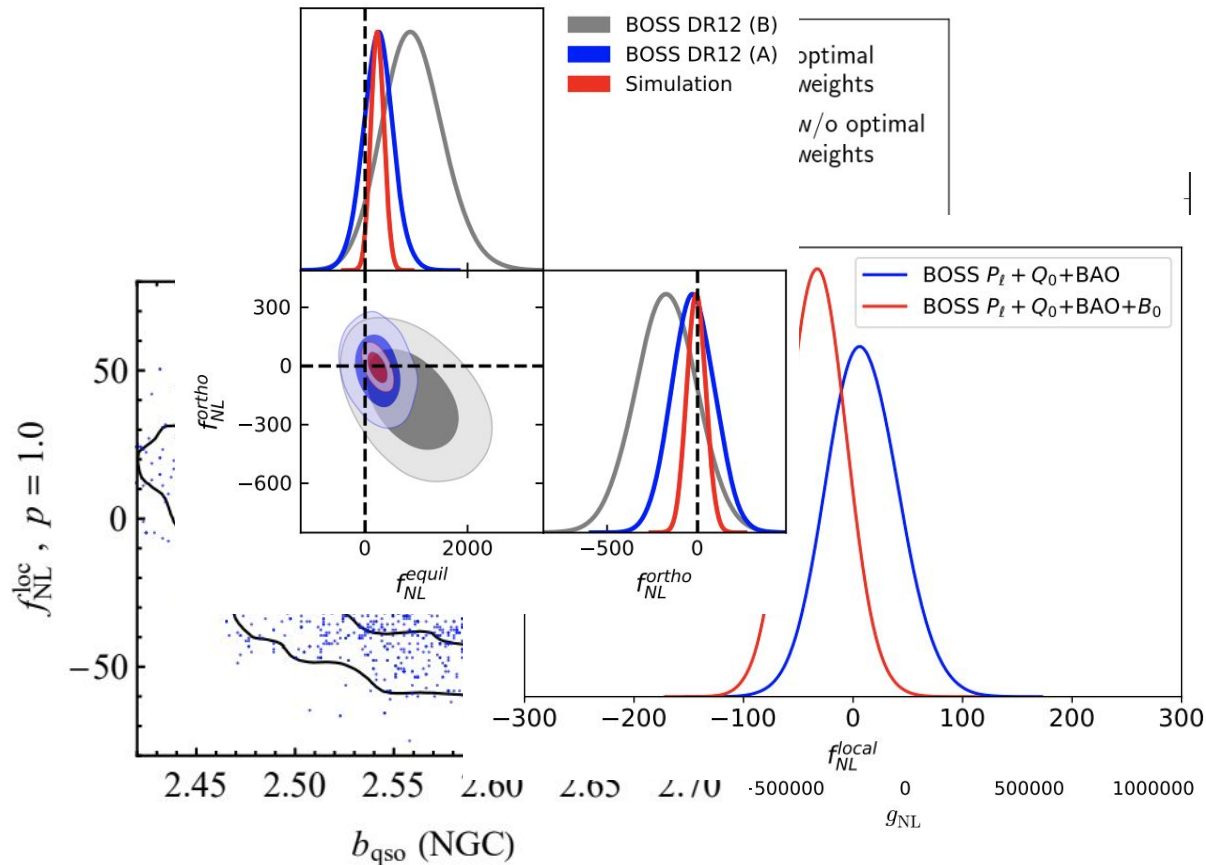
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Cabass++22a



# LSS $f_{NL}^{(loc)}$ Constraints - BOSS LRGs

Slosar++08

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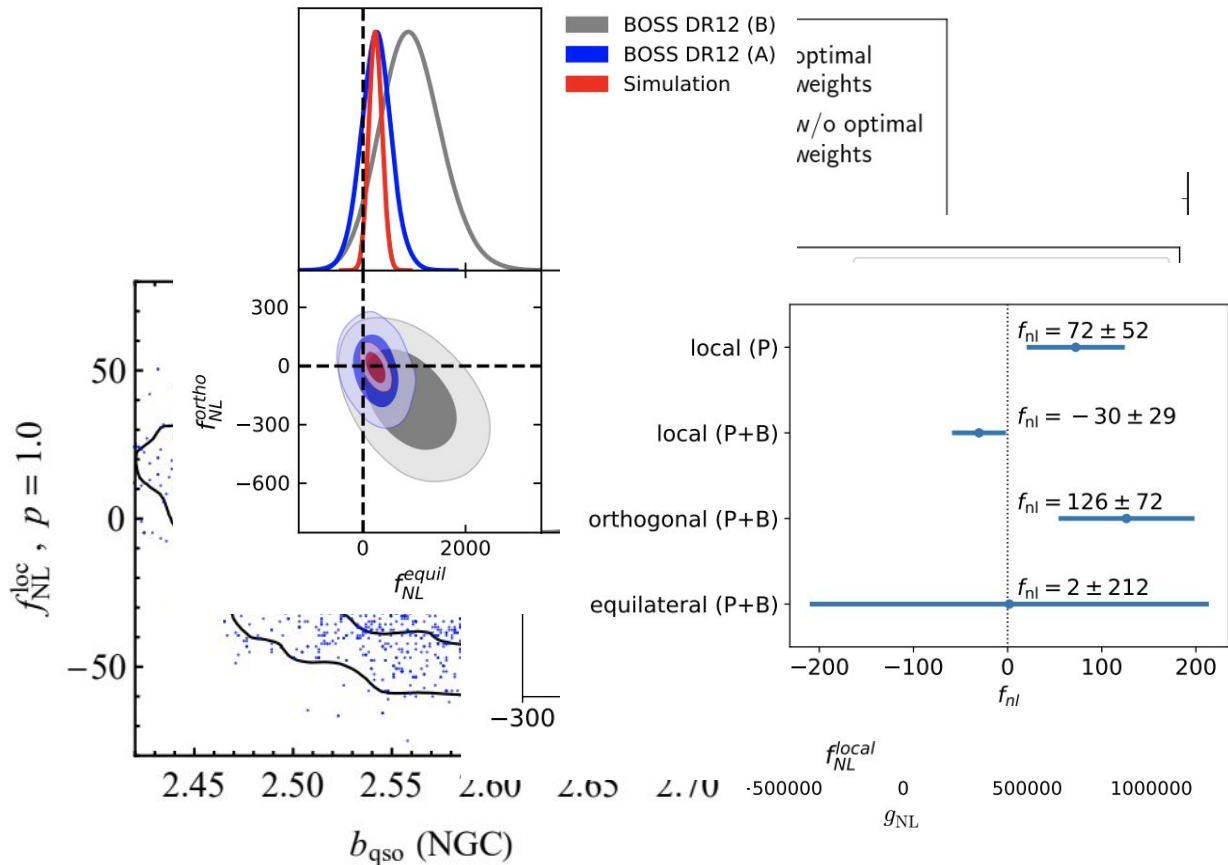
Castorina++19

Mueller++21

D'Amico++22

Cabass++22a

$\rightarrow \sigma(f_{NL}^{(loc)}) \gtrsim 20$





# LSS $f_{NL}^{(loc)}$ Constraints - BOSS LRGs

Slosar++08

Ross++12

Leiste

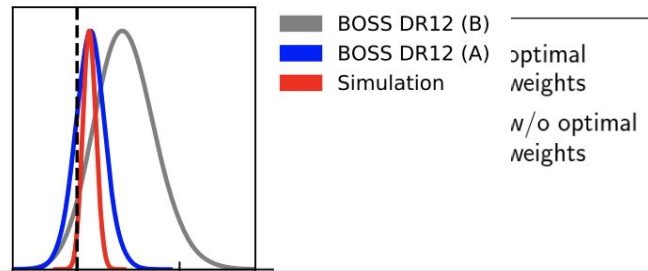
Castorina++19

Mueller++21

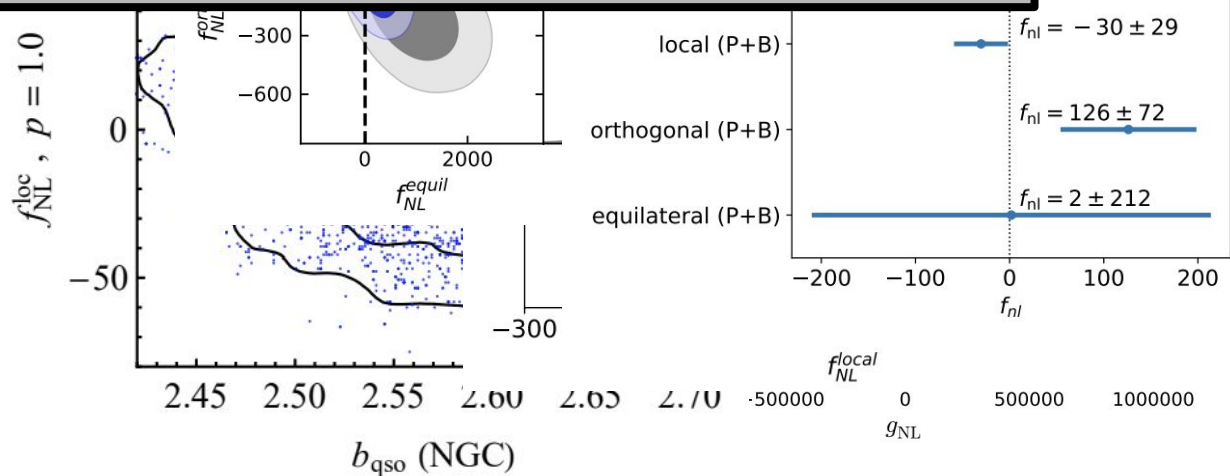
D'Amico++22

Cabass++22a

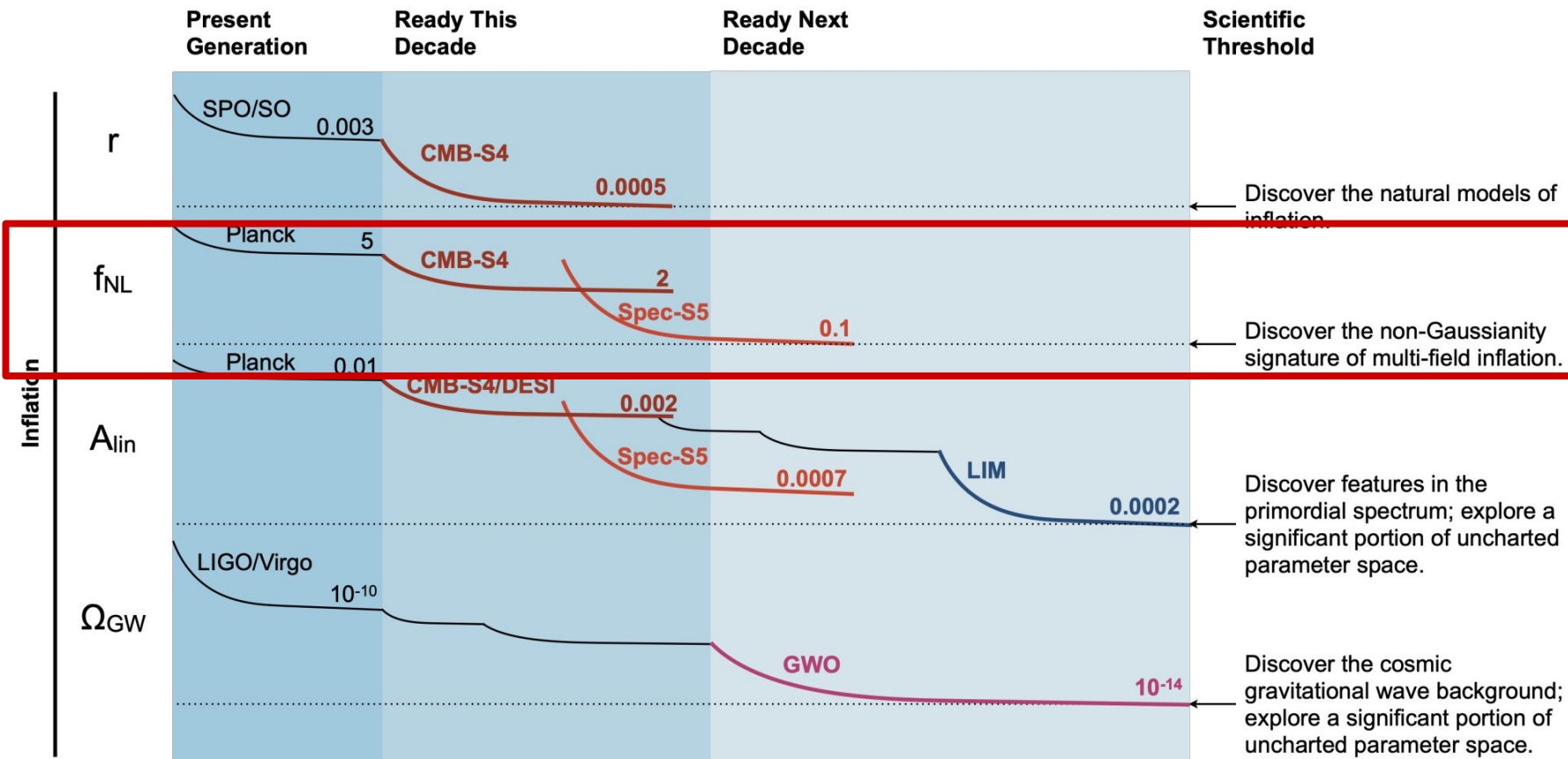
$\rightarrow \sigma(f_{NL}^{(loc)}) \gtrsim 20$



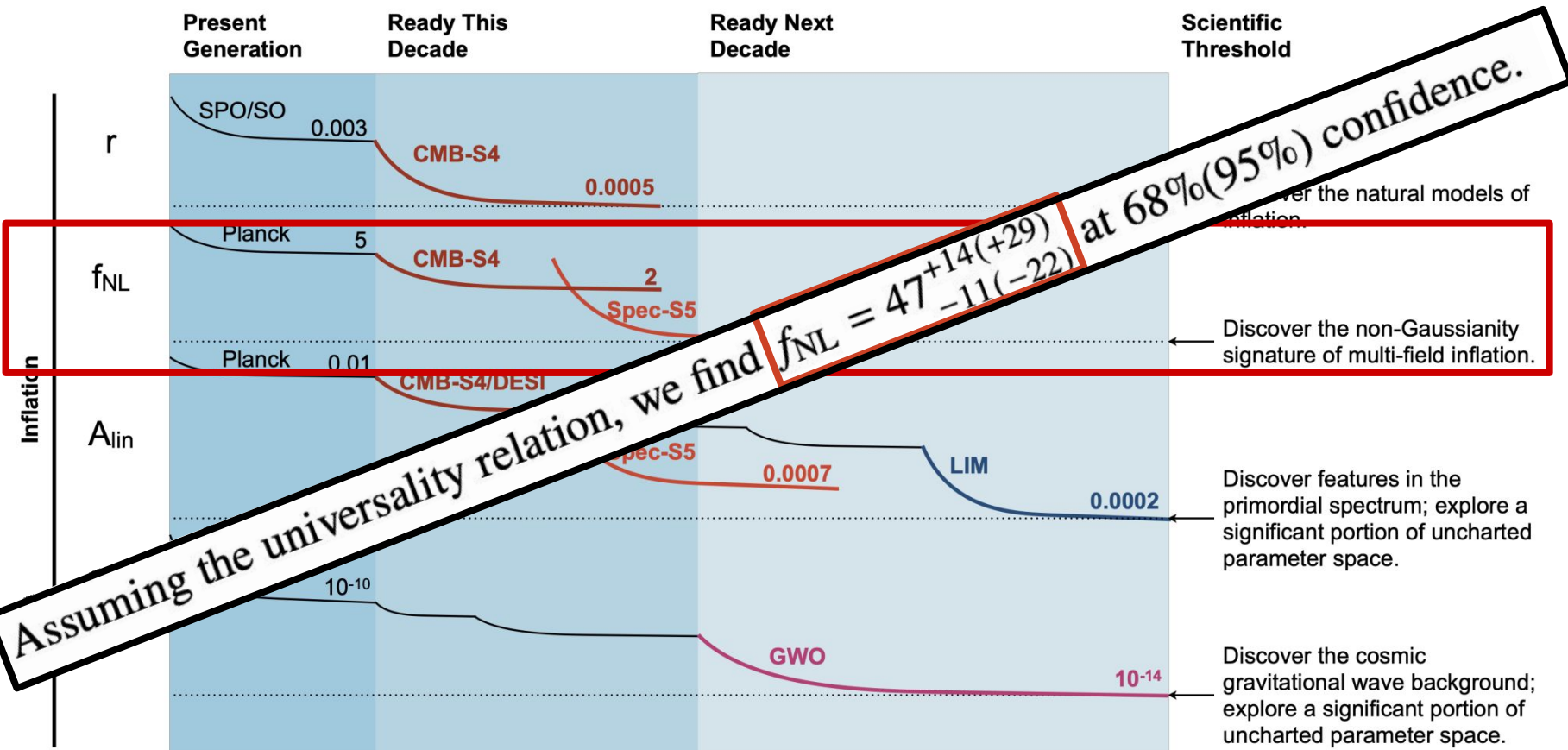
**Best LSS still 4x > Planck**



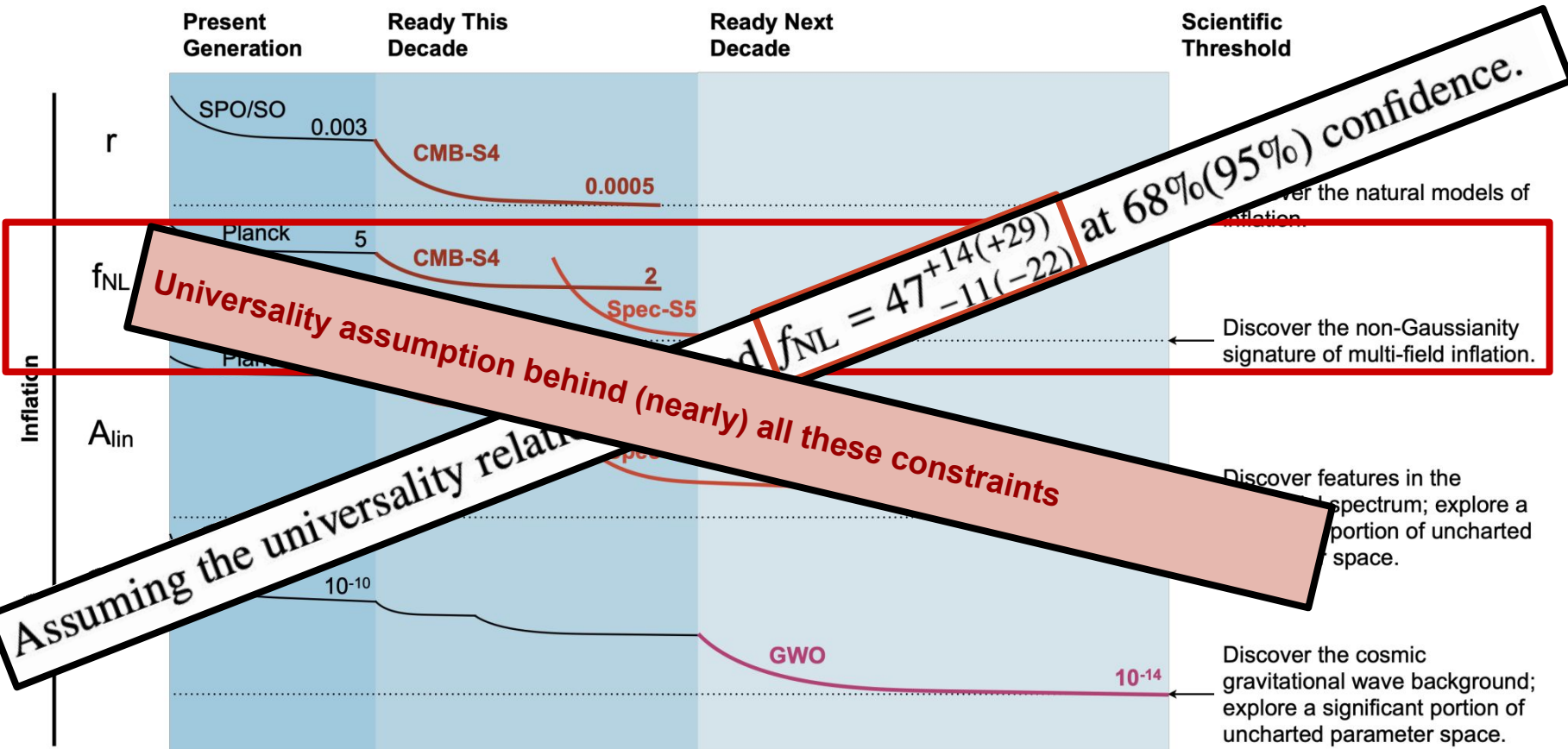
# $f_{NL}$ - A Primary Target for Stage 5 Spectroscopy



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# $f_{NL}$ - A Primary Target for Stage 5 Spectroscopy



# LPNG & Assembly Bias

Universality amounts to 1-1 map between  $b$ ,  $b_\phi$

But  $b_\phi$  is **not** just a function of mass (or  $\sim b$ )!

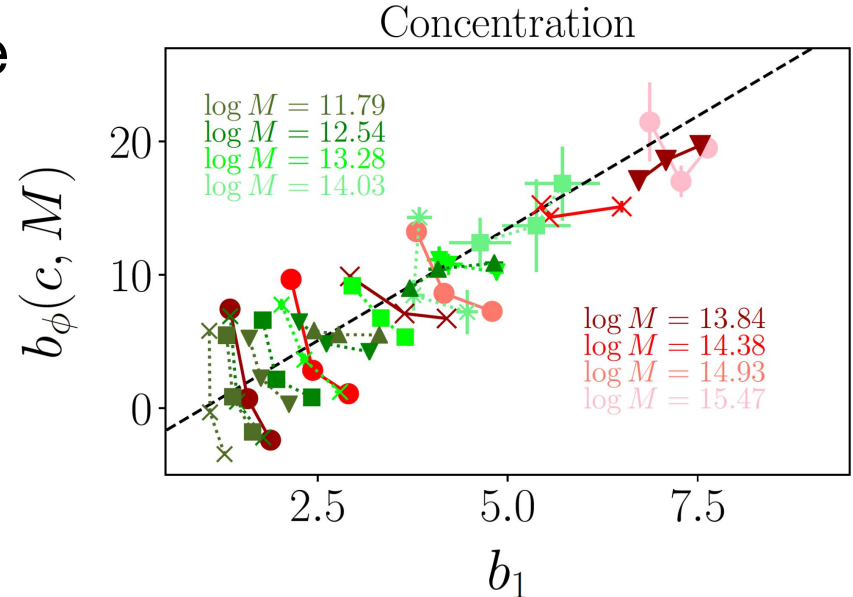
Splits by other quantities change

$b_\phi$  dramatically:

Halo concentration  $c$  has  
a large effect

Can account for this via  $p$ :

$$b_\phi(b, p) \propto b - p$$



# Sub-sample Multi-tracer

---

**Idea:** Identify multi-tracer samples with sub-samples split by concentration (see also Barreira&Krause23)

Multi-tracer technique cancels sample variance

Error on  $f_{NL}$  scales like:

$$\sigma(f_{NL}^{(loc)}) \propto \left( \frac{b_{\phi,1}}{b_1} - \frac{b_{\phi,2}}{b_2} \right)^{-1}$$

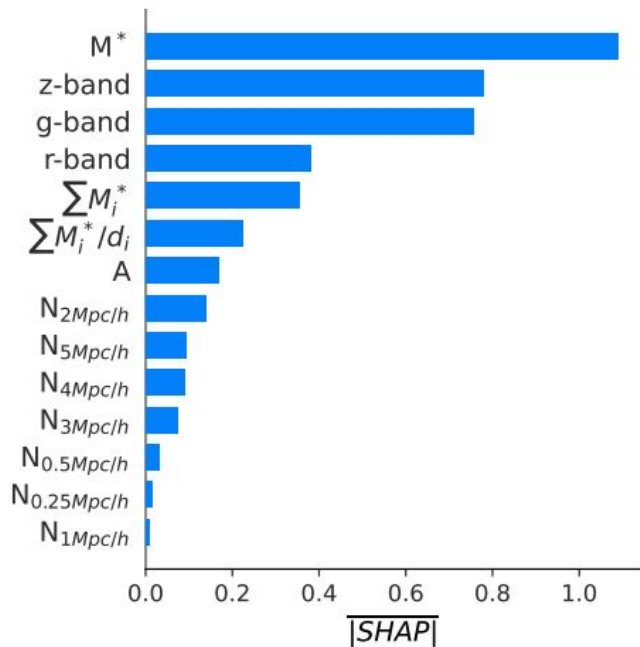
# Multi-tracer forecast procedure

---

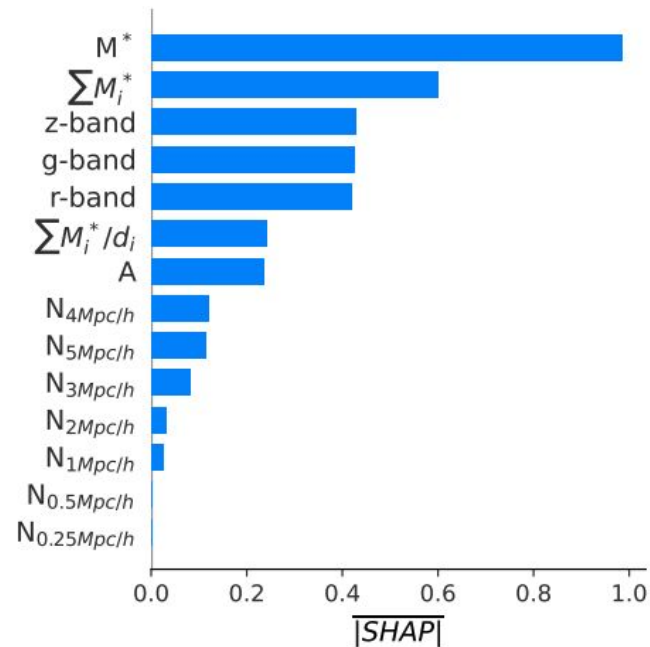
1. Apply LRG/ELG selection cuts to (redshift-space) IllustrisTNG galaxies
2. Train NN to obtain map between galaxy ( $M^*$ ,  $g,r,z$ ,  $\mathbf{s}, \dots$ )  $\rightarrow$  interpolated host halo  $b_\phi$
3. Predict  $b_\phi$  for host halo of each galaxy
4. Divide galaxies into 3 bins by predicted  $b_\phi$

The so-divided bins are the multi-tracer (MT) samples used in the (linear) Fisher forecast - usual caveats

# Feature Importance



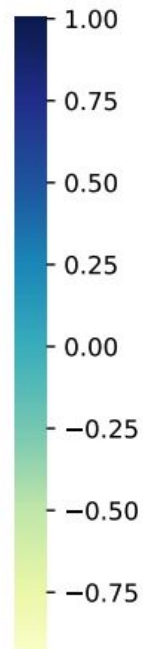
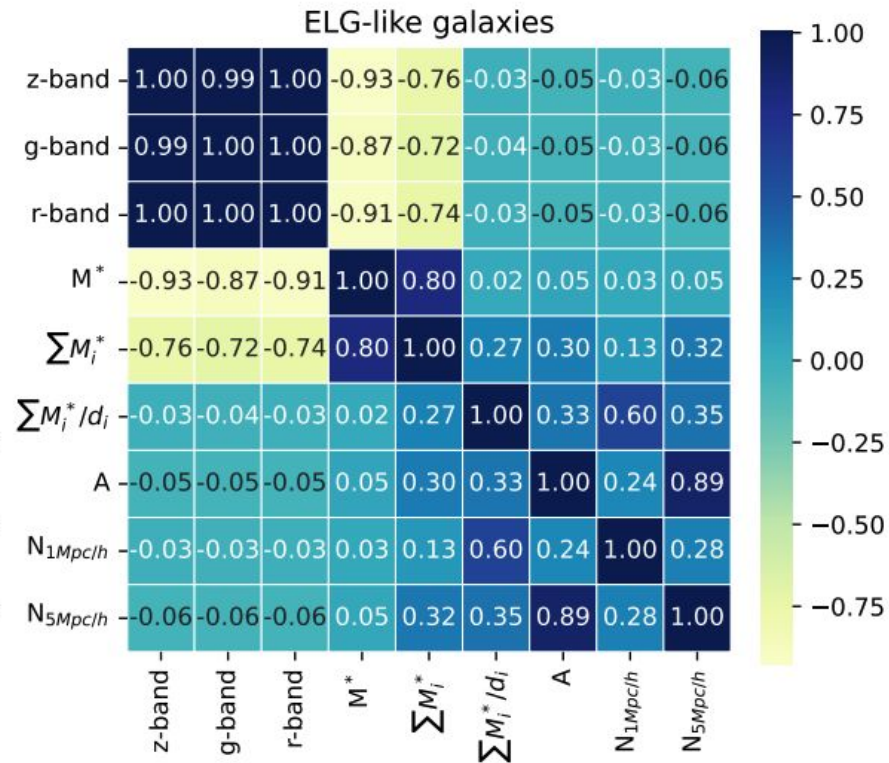
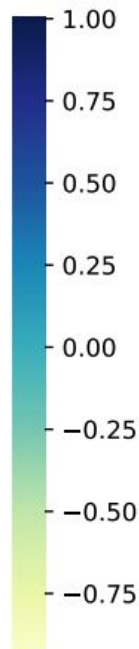
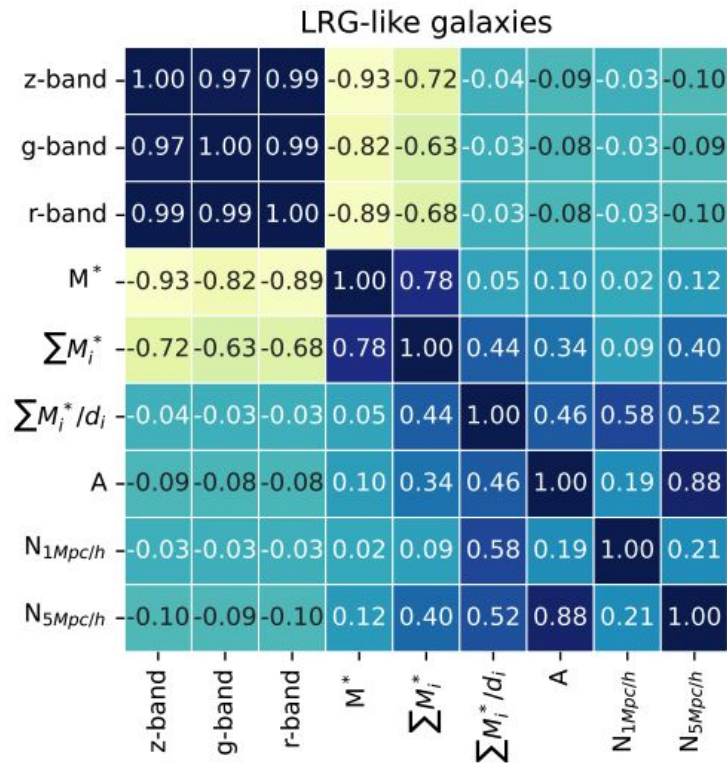
(a) ELG-like galaxies



(b) LRG-like galaxies



# Pearson Correlation



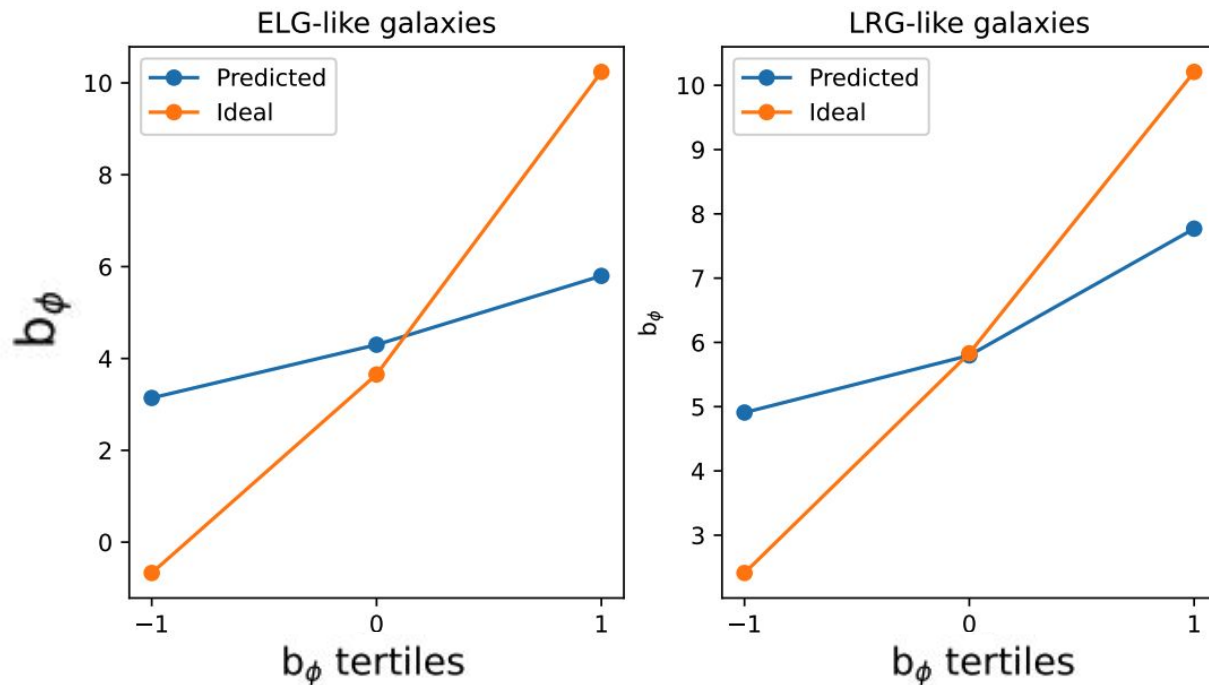
# Results in split bins

**Predicted** - ML result

**Ideal** - perfect recovery

ML model bleeds  
significant info

Still tells us  
something!



# DESI Galaxies

Split each sample  
into tertiles

Tried several  
combinations

Large improvement  
over “naive”  
multitracer!

| ELG + LRG  | $\sigma(f_{NL}^{\text{loc}})$ |
|--|-------------------------------|
| $p = 1$  | 4.0                           |
| (2) ( $\overline{\text{LRG}}$ , $\overline{\text{ELG}}$ ), ideal | 2.3                           |
| (2) ( $\overline{\text{LRG}}$ , $\overline{\text{ELG}}$ ), pred  | 2.3                           |
| (2) (LRG+, ELG+), ideal  | 1.4                           |
| (2) (LRG+, ELG+), pred   | 2.4                           |
| (3) (LRG-, LRG+, ELG-), ideal                                    | 0.8                           |
| (3) (LRG-, LRG+, ELG-), pred                                     | 2.0                           |
| (3) (LRG-, ELG+, ELG-), ideal                                    | 0.8                           |
| (3) (LRG-, ELG+, ELG-), pred                                     | 2.0                           |
| (3) (LRG-, ELG+, else), ideal                                    | 0.6                           |
| (3) (LRG-, ELG+, else), pred                                     | 1.5                           |

# Future LPNG Surveys - MT vs ST

---

Recall:

$$\sigma(f_{\text{NL}}^{(\text{loc})}) \propto \left( \frac{b_{\phi,1}}{b_1} - \frac{b_{\phi,2}}{b_2} \right)^{-1}$$

$$b_{\phi}(b, p) \propto b - p$$

Simplify and  
assume fixed  $b$ :

$$\sigma(f_{\text{NL}}^{(\text{loc})}) \xrightarrow{\text{same } b} (\Delta p)^{-1}$$

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What shape of MT vs ST should we expect?

# Future LPNG Surveys - MT vs ST

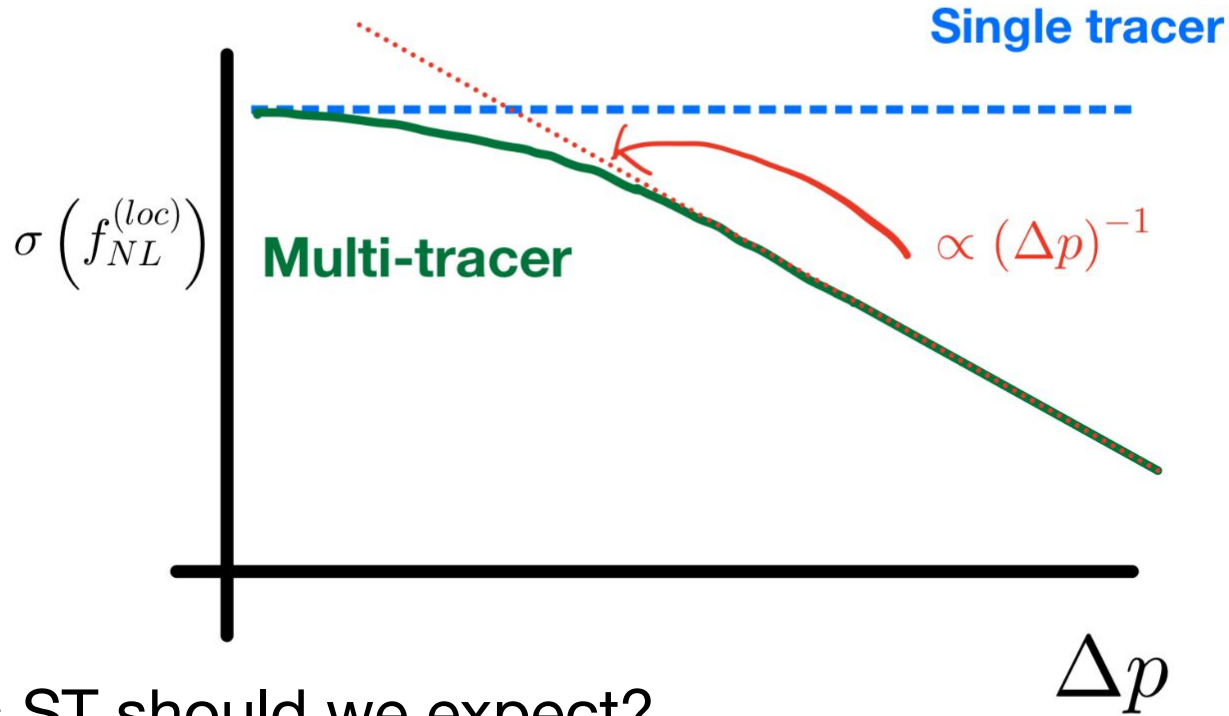
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Simplify and  
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What shape of MT vs ST should we expect?

# SPHEREx - Forecast assumptions

---

Linear redshift space power spectrum

Redshift range:  $0.1 < z < 3.0$

$$f_{\text{sky}} = 0.65$$

$$k_{\text{min}} = 0.001 \text{ h/Mpc}$$

Agree with Sailer++21 on single-tracer

Redshift errors:

$$\exp\left(-\left[k\mu\sigma_z\frac{d\chi}{dz}\right]^2\right)$$

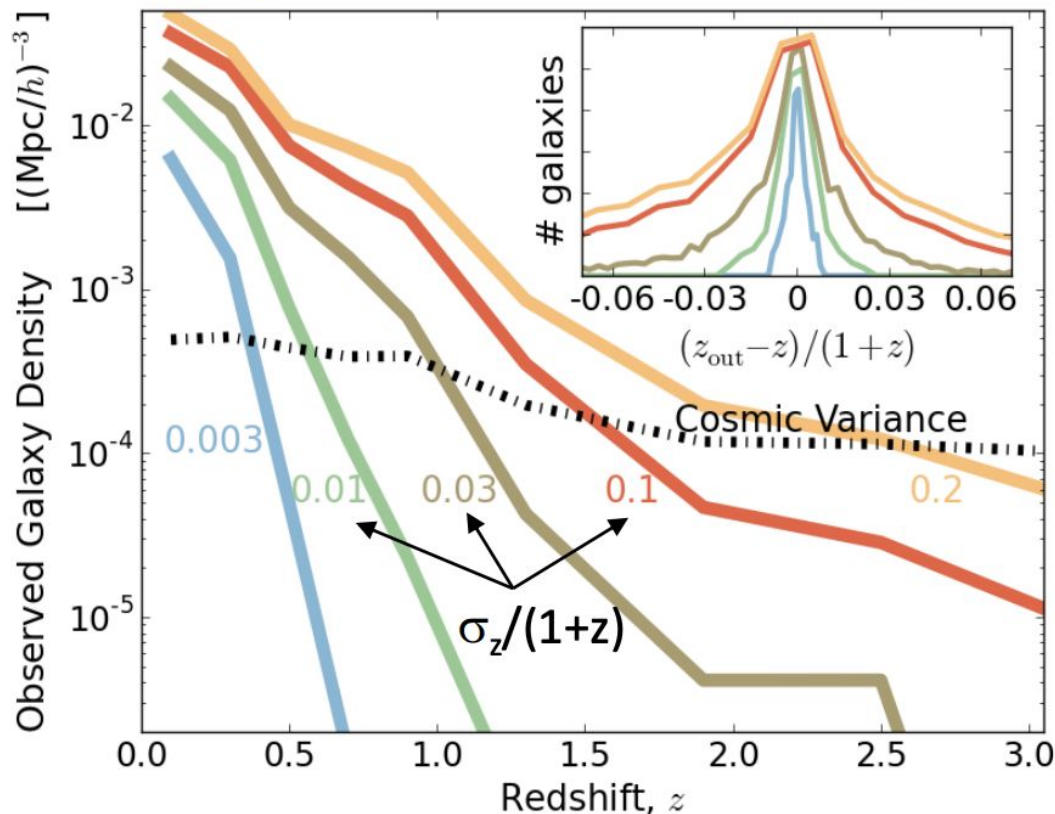
# SPHEREx - Redshift error samples

Use various combos  
of all 5 samples

Combos weighted  
by bias (following  
Doré+14)

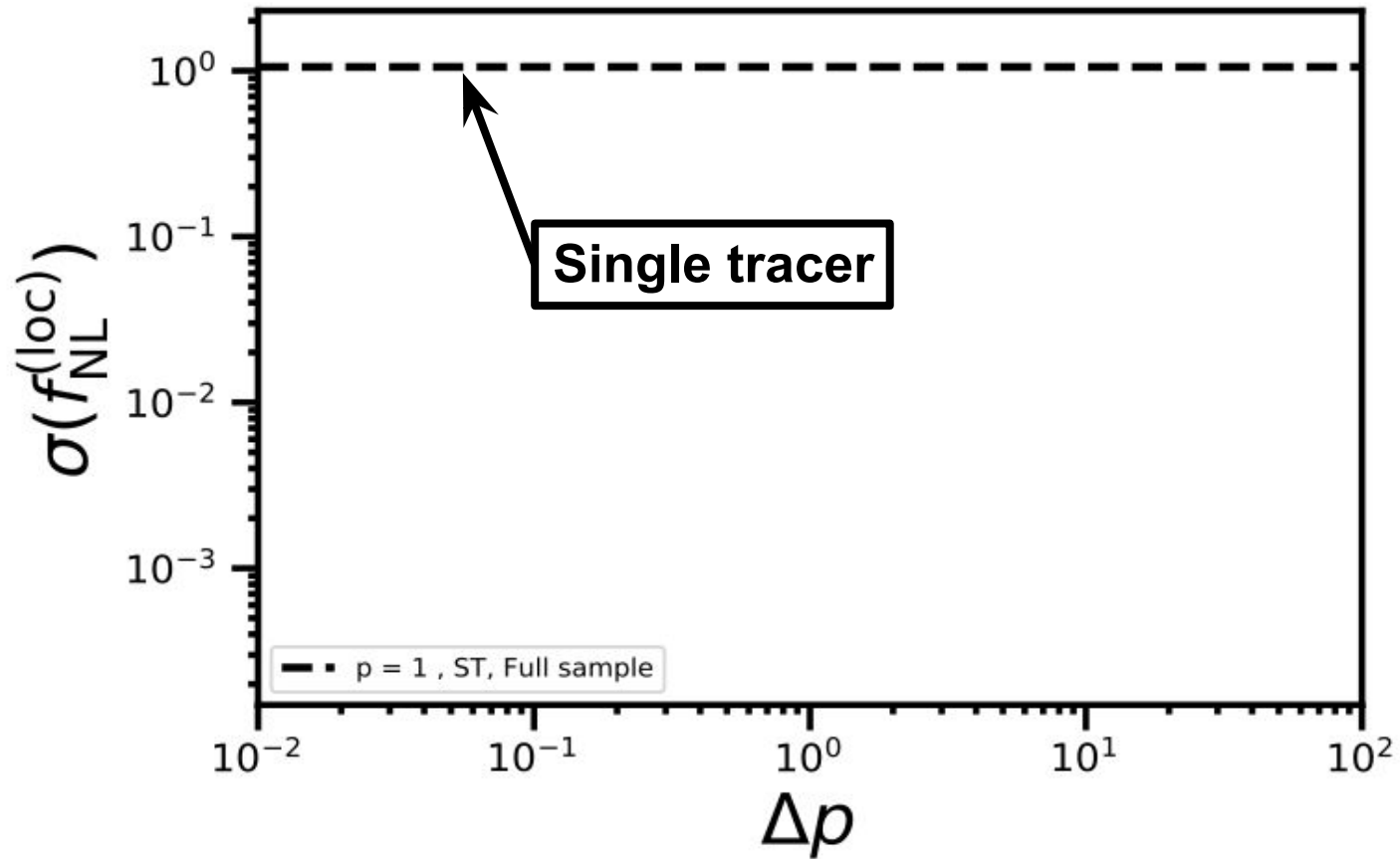
Always assume most  
conservative redshift  
error for combos

Catalog Split into Redshift Accuracy Bins

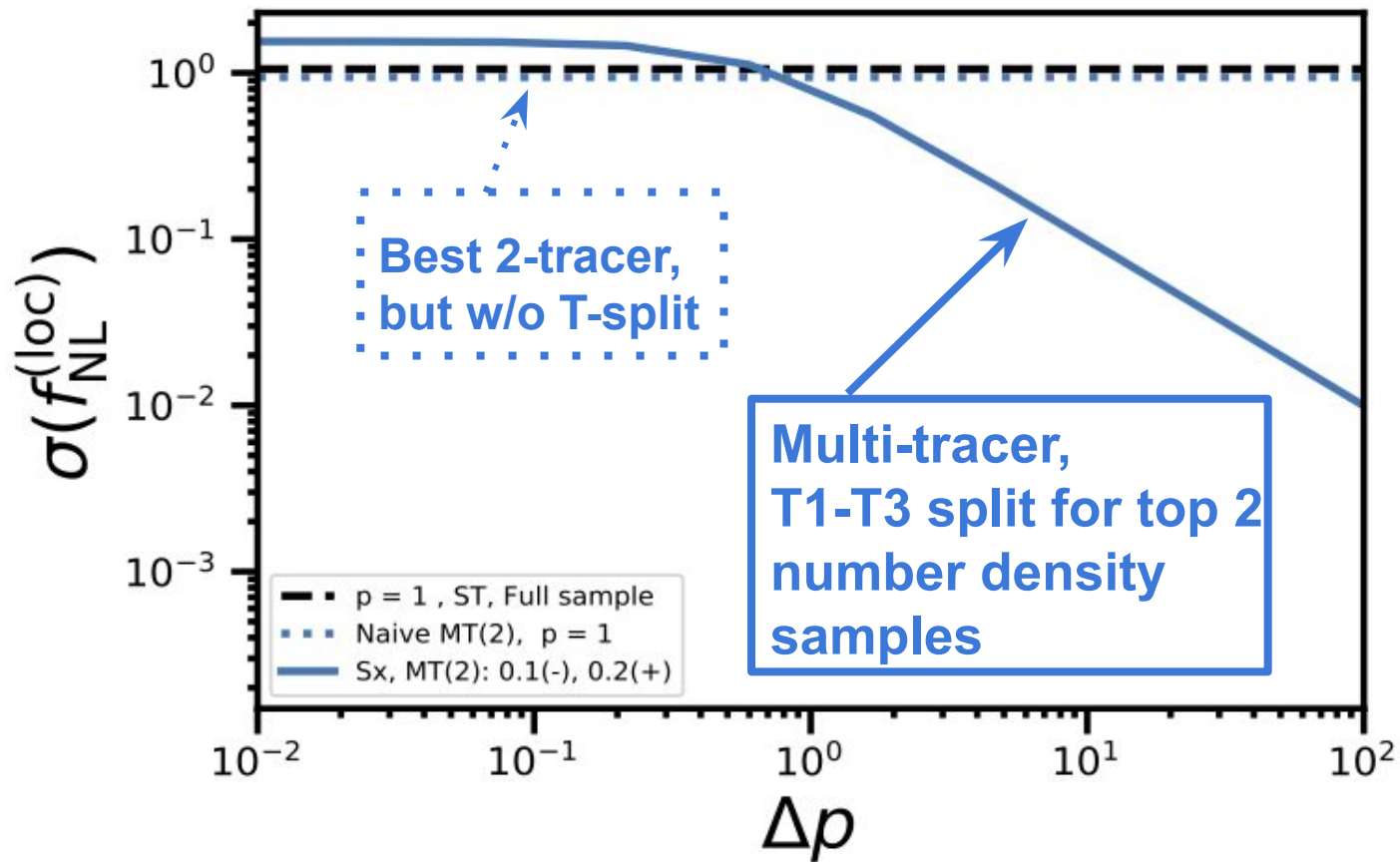




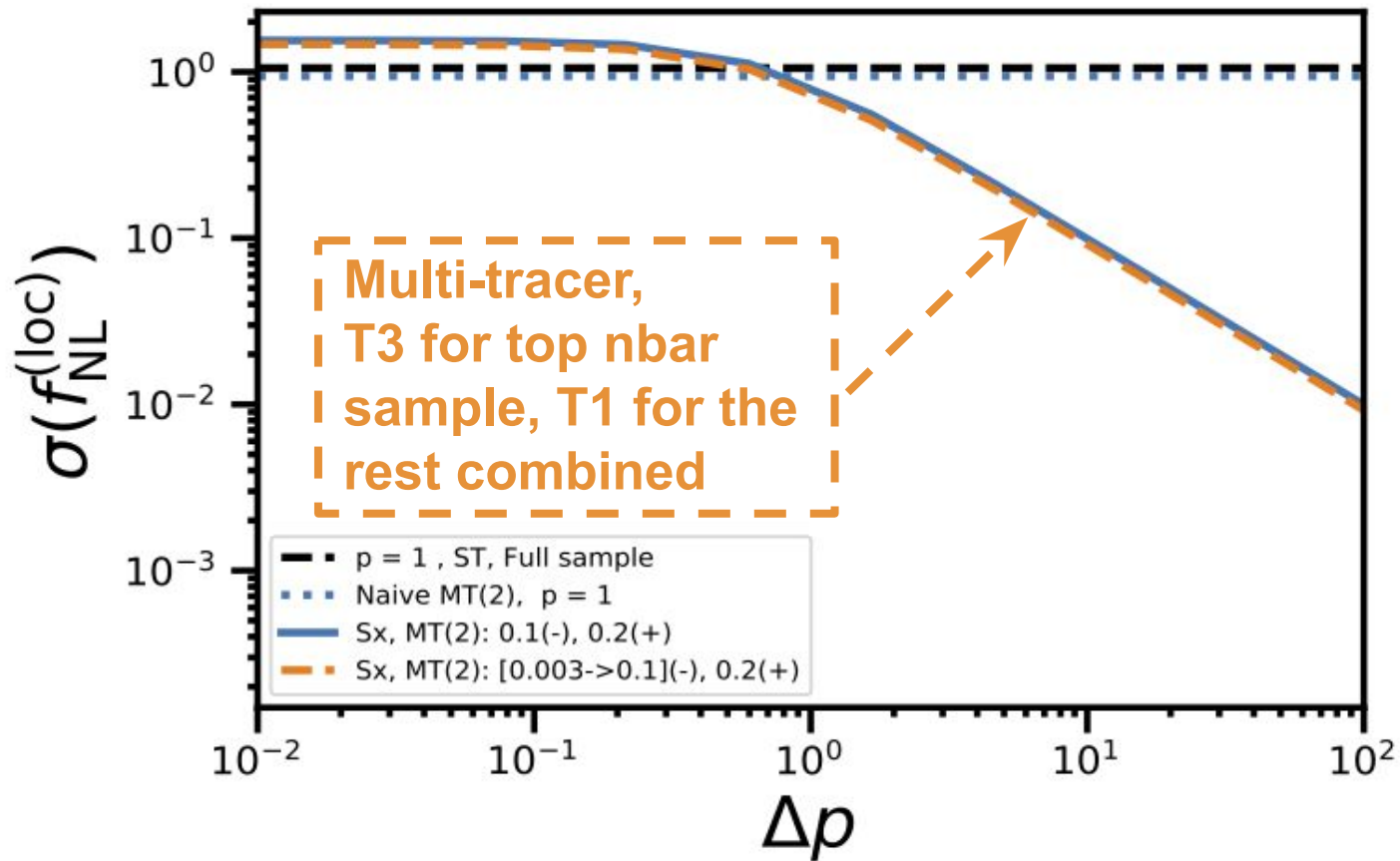
# Single-tracer - combined sample



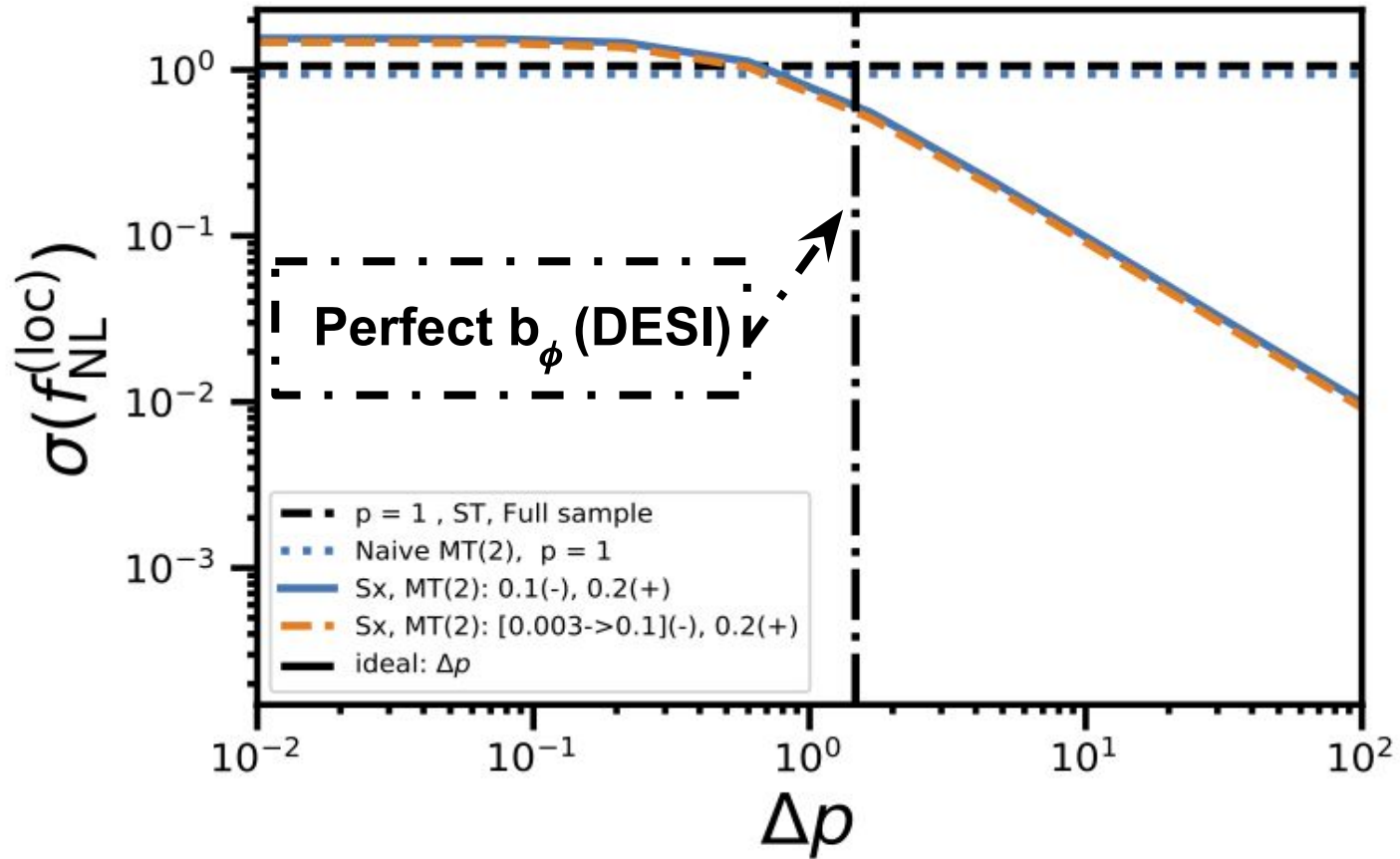
# 2 individual tracers



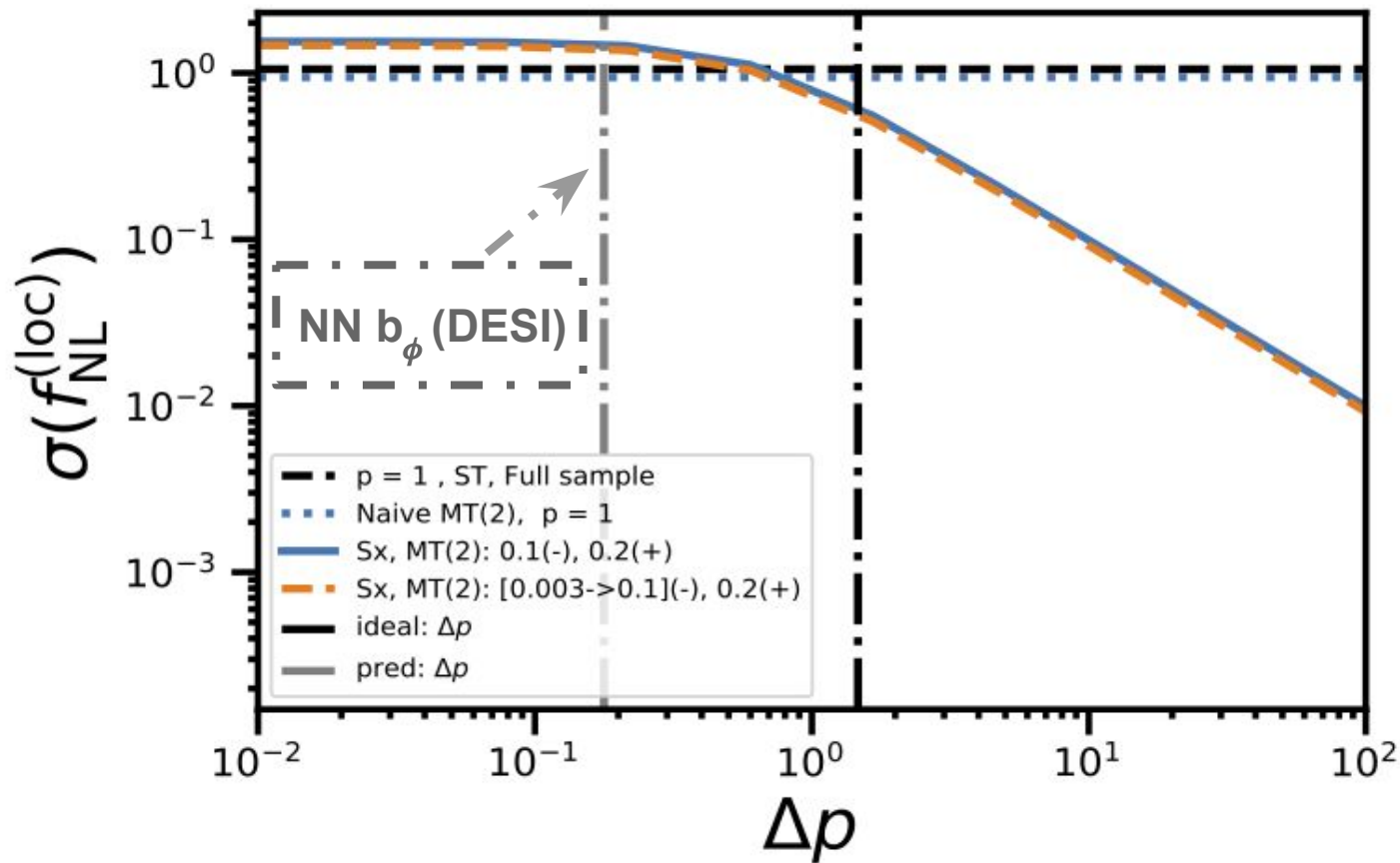
# 2-tracer combination



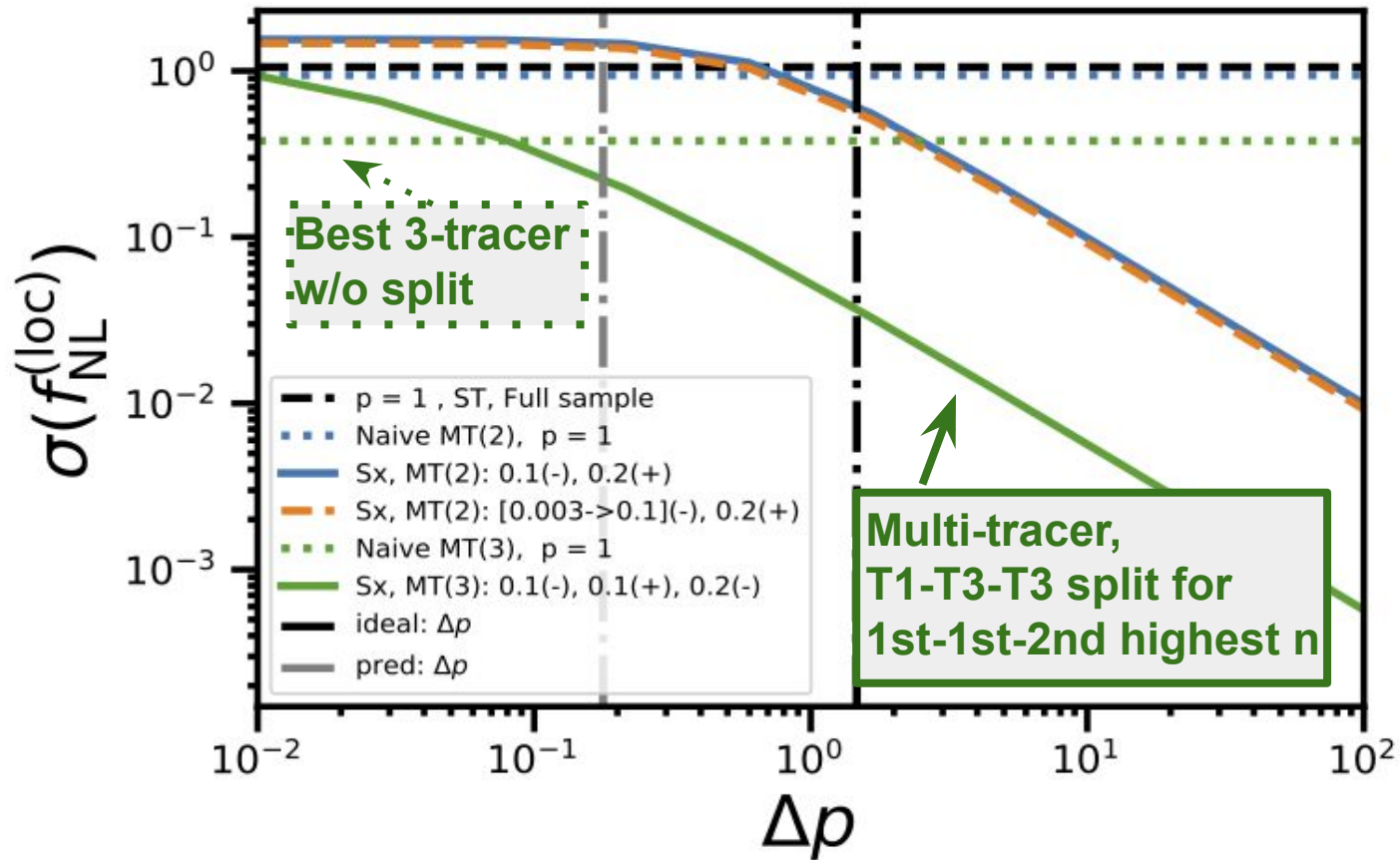
# What we aspire to



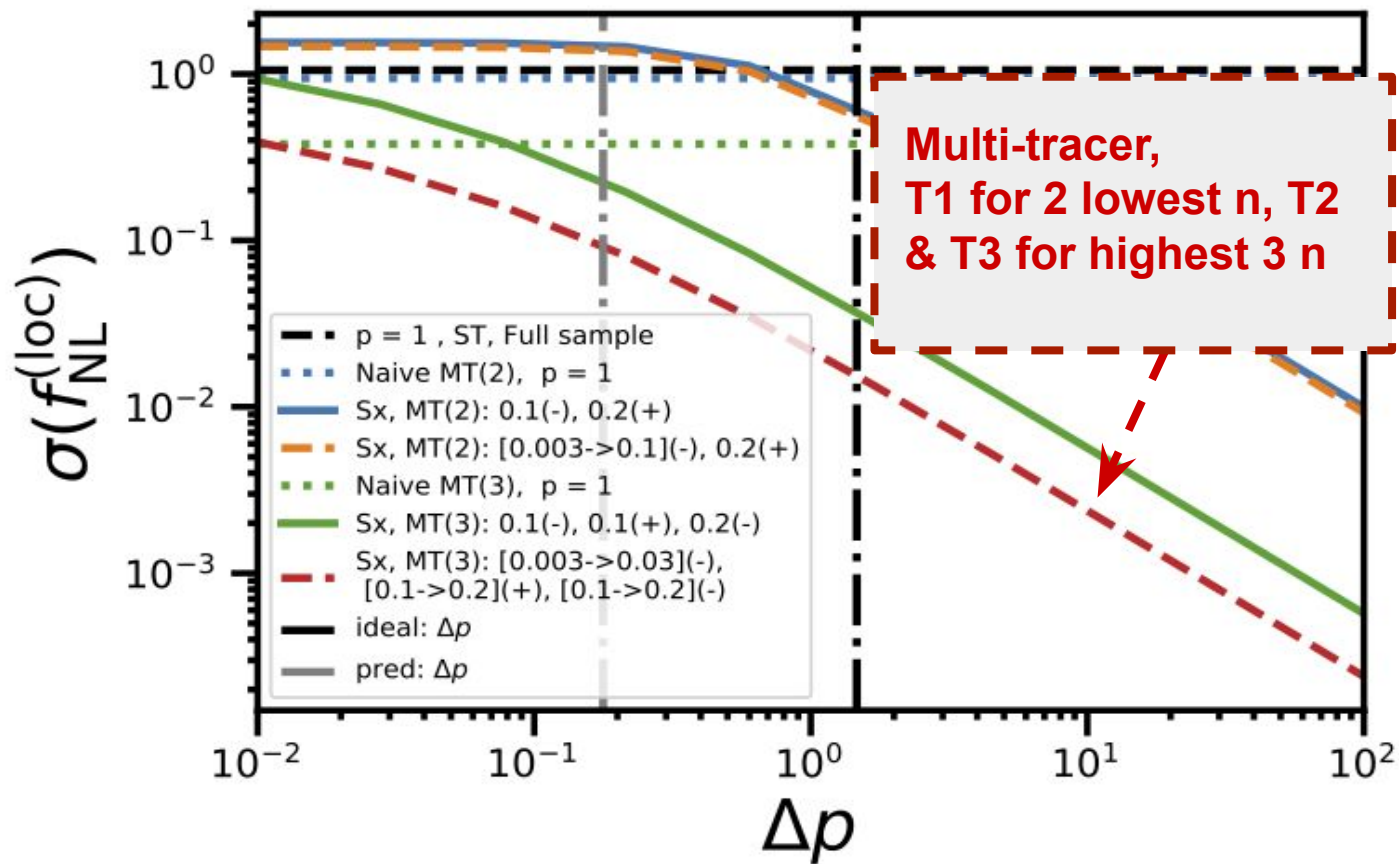
# What we might get



# 3 individual tracers



# 3-tracer combination



# Summary

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LPNG with assembly bias underappreciated until recently

Multi-tracer on subsamples can drastically **reduce**  $\sigma(f_{NL})$

For DESI, **3x improvement** over single-tracer with ML

Further factor of 2x improvement possible if better model

Future surveys may benefit **by >10x**

Of course, now we need to go **beyond Fisher!**